Qualitative Analysis for Nonlinear Differential Equations
Math 102 Section 107

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D. $P(t) = e^{0t}$ and $P(t) = e^{\frac{a}{b}t}$

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